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Physics Letters B

www.elsevier.com/locate/physletbCharmed tetraquarks T_{cc} and T_{cs} from dynamical lattice QCD simulations [☆]Yoichi Ikeda ^{a,*}, Bruno Charron ^b, Sinya Aoki ^{c,d}, Takumi Doi ^a, Tetsuo Hatsuda ^{a,e}, Takashi Inoue ^f, Noriyoshi Ishii ^d, Keiko Murano ^c, Hidekatsu Nemura ^d, Kenji Sasaki ^d^a Theoretical Research Division, Nishina Center, RIKEN, Saitama 351-0198, Japan^b Department of Physics, The University of Tokyo, Tokyo 113-0033, Japan^c Yukawa Institute of Theoretical Physics, Kyoto University, Kyoto 606-8502, Japan^d Center for Computational Sciences, University of Tsukuba, Ibaraki 305-8571, Japan^e Kavli IPMU (WPI), The University of Tokyo, Chiba 606-8502, Japan^f College of Bioresource Science, Nihon University, Kanagawa 252-0880, Japan

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ABSTRACT

Charmed tetraquarks $T_{cc} = (cc\bar{u}\bar{d})$ and $T_{cs} = (cs\bar{u}\bar{d})$ are studied through the S-wave meson–meson interactions, $D\text{--}D$, $\bar{K}\text{--}D$, $D\text{--}D^*$ and $\bar{K}\text{--}D^*$, on the basis of the $(2+1)$ -flavor lattice QCD simulations with the pion mass $m_\pi \simeq 410, 570$ and 700 MeV. For the charm quark, the relativistic heavy quark action is employed to treat its dynamics on the lattice. Using the HAL QCD method, we extract the S-wave potentials in lattice QCD simulations, from which the meson–meson scattering phase shifts are calculated. The phase shifts in the isospin triplet ($I=1$) channels indicate repulsive interactions, while those in the $I=0$ channels suggest attraction, growing as m_π decreases. This is particularly prominent in the T_{cc} ($J^P=1^+, I=0$) channel, though neither bound state nor resonance are found in the range $m_\pi=410\text{--}700$ MeV. We make a qualitative comparison of our results with the phenomenological diquark picture.

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1. Introduction

One of the long standing challenges in hadron physics is to establish and classify genuine multiquark states other than baryons (3 quark states) and mesons (quark–antiquark states) [1]. In particular, charmed tetraquarks (such as $T_{cc} (cc\bar{u}\bar{d})$, $T_{cs} (cs\bar{u}\bar{d})$) and bottomed tetraquarks (such as T_{bb} , T_{bc} , T_{bs}) are unambiguous candidates for such multiquark states [2–5], since there are no annihilations among the four quarks. If they form bound states or resonances with respect to the corresponding two-meson thresholds, they could be experimentally observed in B -factories and relativistic heavy-ion colliders [6–9].

In this Letter, we exclusively investigate the charmed tetraquarks T_{cc} and T_{cs} . To understand a possible reason why they may appear as bound states below the two meson threshold, let us consider the diquark picture [10] as a working hypothesis, where $\bar{u}\bar{d}$ in the color $\mathbf{3}$, spin-singlet ($S=0$), isospin-singlet ($I=0$) channel is denoted as a “good” diquark, due to the large attraction between

\bar{u} and \bar{d} generated through a gluon exchange. We now assume that good diquarks are the main substructure of charmed tetraquarks. Then the color-singletness of hadrons and the quark Pauli principle constrain the possible low-mass tetraquarks as follows.

- (i) T_{cc} ($J^P=1^+, I=0$) in which $\bar{u}\bar{d}$ forms a good diquark while the diquark cc with color $\mathbf{3}^*$ and $S=1$ has a weak repulsion between the two charm quarks. This state couples to the $D\text{--}D^*$ system.
- (ii) T_{cs} ($J^P=1^+, I=0$) in which $\bar{u}\bar{d}$ forms a good diquark while the diquark cs with color $\mathbf{3}^*$ and $S=1$ has a weak repulsion. This state couples to the $\bar{K}\text{--}D^*$ system.
- (iii) T_{cs} ($J^P=0^+, I=0$) in which $\bar{u}\bar{d}$ forms a good diquark while the diquark cs with color $\mathbf{3}^*$ and $S=0$ has an attraction. This state couples to the $\bar{K}\text{--}D$ system.

Quantitatively, however, predictions for the binding energies of charmed tetraquarks widely spread, ranging from negative values (resonance) to 100 MeV (deeply bound) with respect to the two-meson thresholds, depending on the details of the dynamical models (diquark model, dynamical four-body calculation in the constituent quark model, meson–meson molecular model, lattice QCD in the heavy-quark limit, etc.) [11–16]. Therefore, a quantitative

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prediction for charmed tetraquarks requires a careful study in full lattice QCD with a finite charm-quark mass.¹

In this Letter, we report our first results on the interactions in the D - D , \bar{K} - D , D - D^* and \bar{K} - D^* systems in $(2+1)$ -flavor lattice QCD simulations. The dynamics of the charm quarks are incorporated on the lattice with the relativistic heavy quark action [19]. The meson-meson scattering phase shifts are derived from the corresponding potentials calculated on the lattice by the HAL QCD method [20–22] (reviewed in [23]), which was recently shown to be quite accurate to describe some meson-meson scattering phase shifts [24].

This Letter is organized as follows. In Section 2, we present the HAL QCD method to extract the potential between two mesons. We then show the numerical setup of our lattice QCD simulations in Section 3. In Section 4, we show our numerical results for the potentials, from which scattering phase shifts and scattering lengths are extracted for three different quark masses. Section 5 is devoted to a summary and a discussion.

2. HAL QCD method for the meson-meson interaction

In QCD, the two-meson correlation function can be expanded as

$$\begin{aligned} F(\vec{r}, t) &\equiv \sum_{\vec{x}} \langle 0 | \mathcal{O}_{h_1}(\vec{x} + \vec{r}, t) \mathcal{O}_{h_2}(\vec{x}, t) \bar{\mathcal{J}}_{h_1 h_2}(t=0) | 0 \rangle \\ &= \sum_{\vec{x}, n} A_n \langle 0 | \mathcal{O}_{h_1}(\vec{x} + \vec{r}, t) \mathcal{O}_{h_2}(\vec{x}, t) | n \rangle e^{-W_n t} + \dots, \end{aligned} \quad (1)$$

with $A_n = \langle n | \bar{\mathcal{J}}_{h_1 h_2}(t=0) | 0 \rangle$, $\bar{\mathcal{J}}_{h_1 h_2}(t=0)$ stands for a source operator at $t_{\text{src.}} = 0$ which creates two meson states and $\mathcal{O}_{h_{1,2}}$ is a point-like interpolating sink operator for the hadron $h_{1,2}$. $W_n = \sqrt{m_1^2 + \vec{k}_n^2} + \sqrt{m_2^2 + \vec{k}_n^2}$ is the relativistic energy of the n -th eigenstate $|n\rangle$ for two mesons, and ellipses represent inelastic contributions.

Consider t sufficiently larger than $t_{\text{src.}}$ that the contributions from elastic scattering states and possible bound states remain while those from inelastic states become negligible. Then, Eq. (1) becomes $F(\vec{r}, t) \rightarrow \sum_n A_n \phi_n(\vec{r}) e^{-W_n t}$, where $\phi_n(\vec{r})$ is an equal-time Nambu-Bethe-Salpeter (NBS) wave function [25], from which the HAL QCD potential U is defined [21] as a solution of

$$H_0 \phi_n(\vec{r}) + \int d\vec{r}' U(\vec{r}, \vec{r}') \phi_n(\vec{r}') = E_n \phi_n(\vec{r}), \quad (2)$$

for all elastic eigenstates n , where $H_0 = -\nabla^2/2\mu$ with $\mu = m_1 m_2 / (m_1 + m_2)$ and $E_n = \vec{k}_n^2/2\mu$ is a kinetic energy. Here the non-local but n -independent potential $U(\vec{r}, \vec{r}')$ can be shown to exist, by explicitly constructing it as

$$U(\vec{r}, \vec{r}') = \sum_n (E_n - H_0) \phi_n(\vec{r}) \cdot \tilde{\phi}_n^*(\vec{r}'), \quad (3)$$

where $\tilde{\phi}_n^*(\vec{r}')$ is the dual basis associated with $\phi_n(\vec{r}')$, and the summation over n is restricted to elastic channels. (For details and proofs, see [21,23].)

In principle, the potential is extracted from $F(\vec{r}, t)$ at large t , when it is dominated by the $n=0$ state (i.e. the ground state) contribution [21,23]. In practice, however, $F(\vec{r}, t)$ is usually noisier at larger t , so that an accurate determination of potentials in this way becomes difficult.

To overcome this practical difficulty, an alternative method has been proposed in [22]. Since $U(\vec{r}, \vec{r}')$ is n -independent by definition, a normalized correlation function $R(\vec{r}, t) = F(\vec{r}, t)/e^{-(m_1+m_2)t}$ satisfies

$$\begin{aligned} \left(-\frac{\partial}{\partial t} - H_0\right) R(\vec{r}, t) &= \sum_n A_n (\Delta W_n - H_0) \phi_n(\vec{r}) e^{-\Delta W_n t} \\ &\simeq \sum_n A_n (E_n - H_0) \phi_n(\vec{r}) e^{-\Delta W_n t} \\ &= \int d\vec{r}' U(\vec{r}, \vec{r}') R(\vec{r}', t), \end{aligned} \quad (4)$$

where the non-relativistic approximation that $\Delta W_n \equiv W_n - m_1 - m_2 = E_n + O(k^4/m_1^3, k^4/m_2^3)$ is used.² In the velocity expansion of the non-local potential, we finally obtain the leading order potential as

$$V_{\text{LO}}(\vec{r}) = -\frac{(\partial/\partial t)R(\vec{r}, t)}{R(\vec{r}, t)} - \frac{H_0 R(\vec{r}, t)}{R(\vec{r}, t)}, \quad (5)$$

within the non-relativistic approximation.

To extract S-wave potentials on the lattice, we consider the projection of the normalized correlation function on the A_1^+ representation of the cubic group (containing the $J=0$ representation of the rotational group)

$$R(\vec{r}, t; A_1^+) \equiv P^{(A_1^+)} R(\vec{r}, t) = \frac{1}{24} \sum_{g \in O} \chi^{(A_1^+)}(g) R(g^{-1}\vec{r}, t), \quad (6)$$

where $g \in O$ are elements of the cubic group, and $\chi^{(A_1)}(g) (\equiv 1)$ are the associated characters of the A_1 representation.

3. Numerical setup

We employ $(2+1)$ -flavor full QCD gauge configurations generated by the PACS-CS Collaboration [27,28] on a $32^3 \times 64$ lattice with the renormalization group improved gauge action at $\beta = 1.90$ and the non-perturbatively $O(a)$ -improved Wilson quark action ($C_{\text{SW}} = 1.715$) at $(\kappa_{ud}, \kappa_s) = (0.13754, 0.13640)$, $(0.13727, 0.13640)$, and $(0.13700, 0.13640)$. These parameters correspond to the lattice cutoff $a^{-1} = 2176$ MeV (lattice spacing $a = 0.0907(13)$ fm), determined from π , K and Ω masses as inputs [27], leading to the spatial lattice volume $L^3 \simeq (2.9 \text{ fm})^3$.

As for the charm quark, we employ a relativistic heavy quark (RHQ) action proposed in Ref. [19], which is designed to remove the leading and next-to-leading order cutoff errors associated with heavy quark mass, $\mathcal{O}((m_Q a)^n)$ and $\mathcal{O}((m_Q a)^n (a\Lambda_{\text{QCD}}))$, respectively. The RHQ action is given by

$$S_Q = \sum_{x,y} \bar{Q}(x) D(x,y) Q(y), \quad (7)$$

$$\begin{aligned} D(x,y) &= \delta_{x,y} - \kappa_Q \sum_{i=1}^3 [(r_s - v\gamma_i) U_{x,i} \delta_{x+\hat{i},y} \\ &\quad + (r_s + v\gamma_i) U_{x,i}^\dagger \delta_{x,y+\hat{i}}] \\ &\quad - \kappa_Q [(r_t - v\gamma_4) U_{x,4} \delta_{x+\hat{4},y} + (r_t + v\gamma_4) U_{x,4}^\dagger \delta_{x,y+\hat{4}}] \\ &\quad - \kappa_Q \left[c_B \sum_{i,j} F_{ij} \sigma_{ij} + c_E \sum_i F_{i4} \sigma_{i4} \right] \delta_{x,y}. \end{aligned} \quad (8)$$

¹ The importance of the finite charm-quark mass to extract the c - \bar{c} potentials from lattice QCD was reported previously in [17,18].

² This approximation can be avoided if we allow higher order time derivatives in Eq. (4), whose contribution, however, turns out to be numerically negligible for the systems investigated in this Letter.

Table 1

Parameters of the RHQ action in our calculations. See Ref. [29] for more details.

κ_Q	r_s	ν	c_B	c_E
0.10959947	1.1881607	1.1450511	1.9849139	1.7819512

Parameters of the action are κ_Q , r_s , r_t , ν , c_B and c_E , while the redundant parameter r_t is chosen to be 1. In our simulations, we take the same parameters as in Ref. [29], where the 1S charmonium mass and its relativistic dispersion relation are reproduced. The RHQ parameters are summarized in Table 1.

Periodic boundary conditions are imposed in the three spacial directions, while Dirichlet boundary conditions are taken for the temporal direction at $t/a = \pm 32$ to avoid contaminations from the opposite propagation of mesons in time. Throughout this study, we employ local interpolating operators for mesons, $\phi(x) = \bar{q}(x)\Gamma q(x)$,

Table 2

Meson masses obtained in this study. We employ the scale determined in Ref. [27].

(κ_{ud}, κ_s)	(0.13754, 0.13640)	(0.13727, 0.13640)	(0.13700, 0.13640)
confs.	450	400	399
m_π (MeV)	411(2)	572(2)	699(1)
m_K (MeV)	635(2)	714(1)	787(1)
m_{η_c} (MeV)	2988(2)	3005(1)	3024(1)
$m_{J/\psi}$ (MeV)	3097(2)	3118(1)	3142(1)
m_D (MeV)	1902(3)	1946(1)	1999(1)
m_{D^*} (MeV)	2048(12)	2099(6)	2159(4)

where Γ denotes a 4×4 matrix acting on spinor indices. We take $\Gamma = \gamma_5$ for pseudo-scalar mesons (D and \bar{K}) and $\Gamma = \gamma_i$ for vector mesons (D^*). Meson masses calculated in this work are listed in Table 2 together with the number of configurations used in this work. We measure the correlation function in Eq. (1) with a source

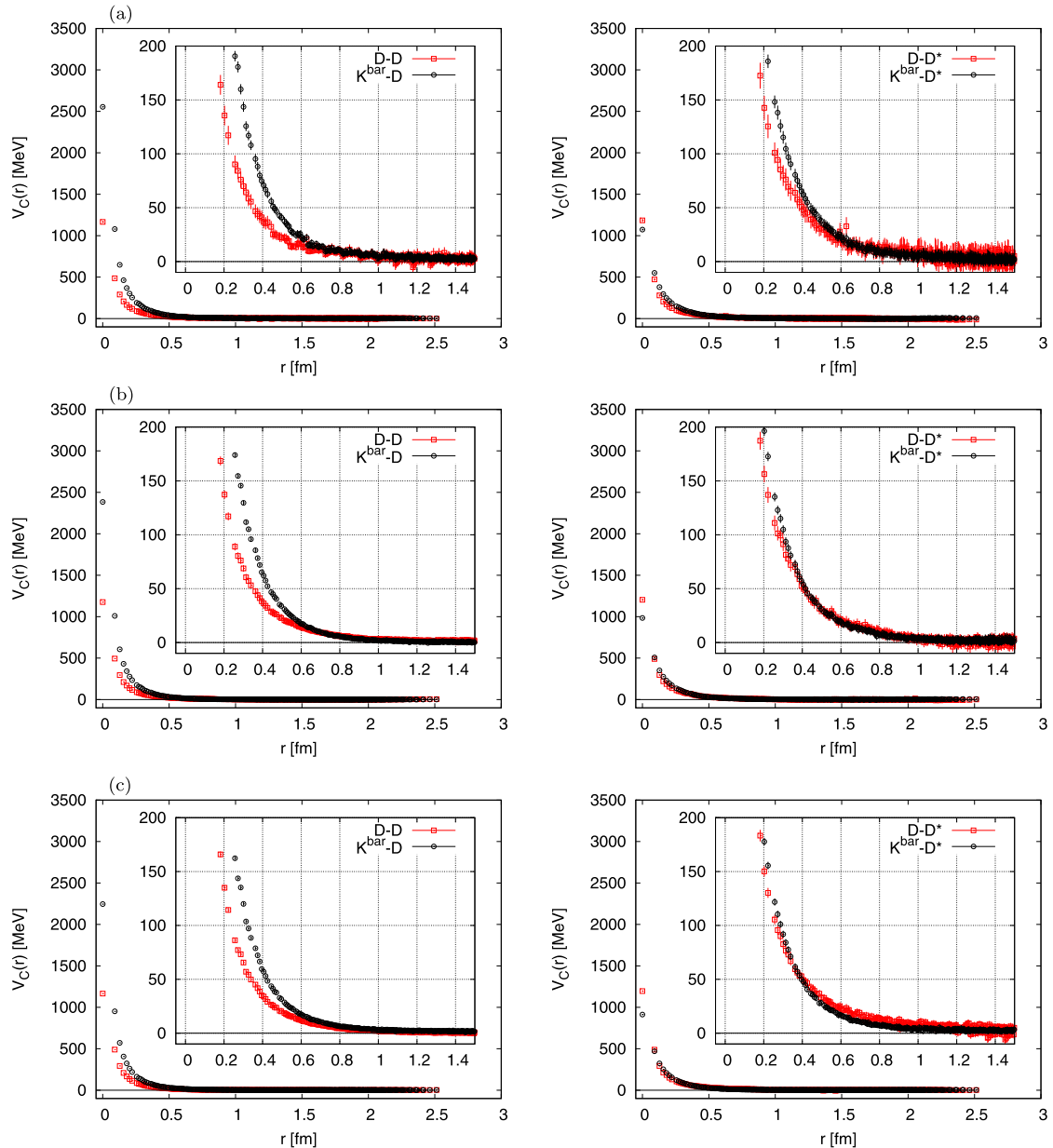


Fig. 1. (Color online.) Left three panels for the S-wave central potentials in the D - D (square) and \bar{K} - D (circle) channels with $(J^P, I) = (0^+, 1)$. Right three panels for the S-wave central potentials in the D - D^* (square) and \bar{K} - D^* (circle) channels with $(J^P, I) = (1^+, 1)$. (a), (b) and (c) are obtained at $m_\pi \simeq 410$ MeV, $m_\pi \simeq 570$ MeV and $m_\pi \simeq 700$ MeV, respectively.

Table 3

The lowest (inelastic) threshold energies for the D - D (D^*-D^*), D - D^* (D^*-D^*), \bar{K} - D (\bar{K}^*-D^*) and \bar{K} - D^* (\bar{K}^*-D) in MeV unit.

Threshold energies	$m_\pi = 411(2)$	$m_\pi = 572(2)$	$m_\pi = 699(1)$
E_{DD}	3805(5)	3893(3)	3999(3)
$E_{D^*D^*}$	4097(23)	4199(11)	4319(7)
E_{DD^*}	3951(12)	4046(6)	4159(5)
$E_{D^*D^*}$	4097(23)	4199(11)	4319(7)
$E_{\bar{K}D}$	2538(3)	2660(2)	2785(2)
$E_{\bar{K}^*D^*}$	3075(15)	3184(9)	3314(8)
$E_{\bar{K}D^*}$	2684(12)	2814(6)	2946(4)
$E_{\bar{K}^*D}$	2930(9)	3031(7)	3153(6)

at one time-slice for each configuration, and the forward and backward propagations are averaged to enhance the statistics. We have checked that the dispersion relation of the 1S charmonium state at

our heaviest pion mass, $m_\pi \sim 700$ MeV, gives a reasonable value of the effective speed of light, $c_{\text{eff}} = 0.987(2)$.

As for the source operators of the D - D , D - D^* , \bar{K} - D and \bar{K} - D^* in isospin I channels, we take the following wall sources:

$$\bar{\mathcal{J}}_{DD}(t=0) = \sum_{\vec{x}_1, \vec{x}_2, \vec{x}_3, \vec{x}_4} [\bar{c}(\vec{x}_1, t) \gamma_5 u(\vec{x}_2, t) \bar{c}(\vec{x}_3, t) \gamma_5 d(\vec{x}_4, t) + (-)^{I+1} \bar{c}(\vec{x}_1, t) \gamma_5 d(\vec{x}_2, t) \bar{c}(\vec{x}_3, t) \gamma_5 u(\vec{x}_4, t)], \quad (9)$$

$$\bar{\mathcal{J}}_{D^*D^*}(t=0) = \sum_{\vec{x}_1, \vec{x}_2, \vec{x}_3, \vec{x}_4} [\bar{c}(\vec{x}_1, t) \gamma_5 u(\vec{x}_2, t) \bar{c}(\vec{x}_3, t) \gamma_5 d(\vec{x}_4, t) + (-)^{I+1} \bar{c}(\vec{x}_1, t) \gamma_5 d(\vec{x}_2, t) \bar{c}(\vec{x}_3, t) \gamma_5 u(\vec{x}_4, t)], \quad (10)$$

$$\bar{\mathcal{J}}_{\bar{K}D}(t=0) = \sum_{\vec{x}_1, \vec{x}_2, \vec{x}_3, \vec{x}_4} [\bar{s}(\vec{x}_1, t) \gamma_5 u(\vec{x}_2, t) \bar{c}(\vec{x}_3, t) \gamma_5 d(\vec{x}_4, t) + (-)^{I+1} \bar{s}(\vec{x}_1, t) \gamma_5 d(\vec{x}_2, t) \bar{c}(\vec{x}_3, t) \gamma_5 u(\vec{x}_4, t)], \quad (11)$$

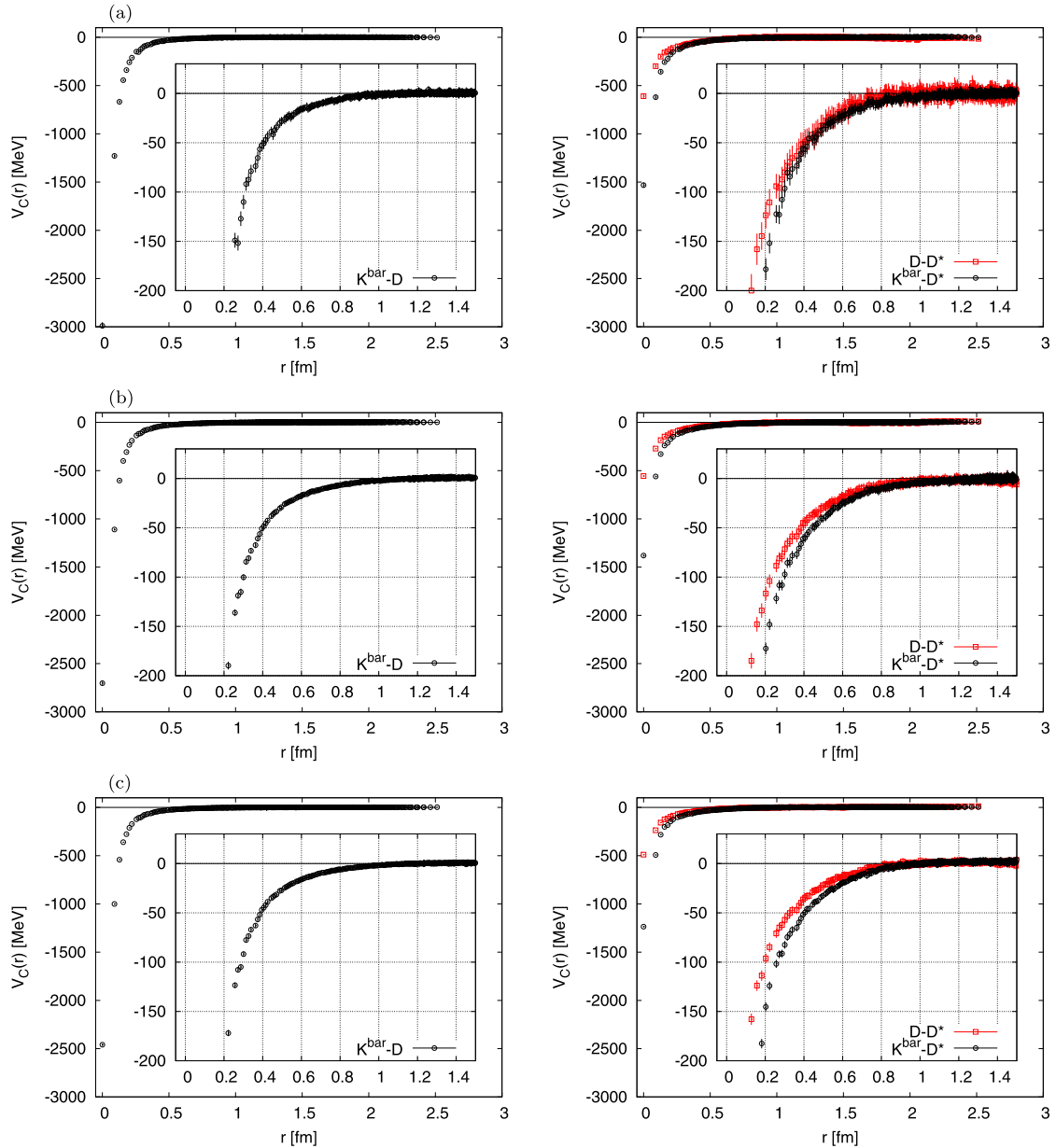


Fig. 2. (Color online.) Left three panels for the S-wave central potentials in the \bar{K} - D channel with $(J^P, I) = (0^+, 0)$. Right three panels for the S-wave central potentials in the D - D^* (square) and \bar{K} - D^* (circle) channels with $(J^P, I) = (1^+, 0)$. (a), (b) and (c) are obtained at $m_\pi \simeq 410$ MeV, $m_\pi \simeq 570$ MeV and $m_\pi \simeq 700$ MeV, respectively.

$$\begin{aligned} \tilde{\mathcal{J}}_{\bar{K}D^*}(t=0) = & \sum_{\vec{x}_1, \vec{x}_2, \vec{x}_3, \vec{x}_4} [\bar{s}(\vec{x}_1, t) \gamma_5 u(\vec{x}_2, t) \bar{c}(\vec{x}_3, t) \gamma_i d(\vec{x}_4, t) \\ & + (-)^{I+1} \bar{s}(\vec{x}_1, t) \gamma_5 d(\vec{x}_2, t) \bar{c}(\vec{x}_3, t) \gamma_i u(\vec{x}_4, t)]. \quad (12) \end{aligned}$$

4. Meson–meson potentials and scattering phase shifts

With the above setup, we study the S-wave meson–meson interactions in the following channels related to T_{cc} and T_{cs} with $J^P = 0^+, 1^+$: $D\text{--}D$ ($J^P = 0^+, I = 1$), $\bar{K}\text{--}D$ ($J^P = 0^+, I = 0, 1$), $D\text{--}D^*$ ($J^P = 1^+, I = 0, 1$), and $\bar{K}\text{--}D^*$ ($J^P = 1^+, I = 0, 1$). We show the potentials calculated from Eq. (5) at the time-slice $t/a = 16$. Since the energy differences between the elastic and inelastic thresholds are 200–300 MeV as shown in Table 3, the inelastic contributions in Eq. (1) are expected to be suppressed in the time-slices $t/a > 11$.

In Fig. 1, we show our results for the S-wave meson–meson potentials in the $I = 1$ channels with $J^P = 0^+$ (left panels) and $J^P = 1^+$ (right panels). We find that all the potentials in the $I = 1$ channel are repulsive at all distances. This observation is consistent with the absence of good $\bar{u}d$ diquarks in the $I = 1$ channel, as discussed in the Introduction. Since the quark mass dependence of the potentials is rather weak, it is unlikely that interactions in these channels turn into strong attractions to form bound states even at the physical quark mass. Phenomenological models also predict the absence of bound states in the $I = 1$ channels.

In Fig. 2, we show our results for the S-wave meson–meson central potentials in the $I = 0$ channels with $J^P = 0^+$ (left panels) and $J^P = 1^+$ (right panels). Contrary to the previous results in the $I = 1$ channels, all the potentials in the $I = 0$ channels show attractions at all distances without repulsive core. In addition, we find that all potentials become more attractive as the pion mass decreases, and the attraction at short distance ($r = 0.2\text{--}0.3$ fm) in the $\bar{K}\text{--}D$ channel is stronger than in the $D\text{--}D^*$ and $\bar{K}\text{--}D^*$ channels. Such tendency is again consistent with the existence of good $\bar{u}d$ diquarks in the $I = 0$ channel, as discussed in Section 1.

To investigate the possible existence of bound states or resonances in the $I = 0$ channels, we fit the potentials with analytic functions of r and solve the Schrödinger equation with the fitted potentials at a given time-slice. We employ a multi-range Gaussian form to fit the potential, namely $g(r) \equiv \sum_{n=1}^{N_{\max}} V_n \cdot \exp(-v_n r^2)$ with V_n and v_n being fit parameters. For all cases, we obtain good fits with $\chi^2/\text{d.o.f.} \simeq 0.6$ for $N_{\max} = 4$. Repeating this at different time-slices, the mean values of scattering phase shifts are obtained from the weighted average over the time-slices $t/a = 13$ through 18. Statistical errors for the scattering phase shifts are calculated by the jackknife method, and systematic errors are evaluated by the difference between the weighted average of the phase shifts over the time-slices $t/a = 13\text{--}15$ and $t/a = 16\text{--}18$.

Fig. 3 shows the resultant S-wave scattering phase shifts as a function of the meson–meson center-of-mass energy in the $I = 0$ $\bar{K}\text{--}D$ ($J^P = 0^+$), $\bar{K}\text{--}D^*$ ($J^P = 1^+$) and $D\text{--}D^*$ ($J^P = 1^+$) channels. In Table 4 and Fig. 4, we give the corresponding scattering lengths. We do not find the negative-energy eigenvalues corresponding to the bound state solutions by solving the Schrödinger equation with the potentials shown in Fig. 2. Fig. 3 also indicates that there are no bound states or resonances in this range of pion masses, $m_\pi = 410\text{--}700$ MeV. Although the potentials for $D\text{--}D^*$ and $\bar{K}\text{--}D^*$ are not so much different, as seen in the right panels of Fig. 2, the scattering length in the $D\text{--}D^*$ channel is larger than that in the $\bar{K}\text{--}D^*$ channel. This can be attributed to the smaller kinetic energy of D in comparison to \bar{K} due to a heavier charm quark. A similar tendency has also been reported in studies of phenomenological models (see e.g. [11]).

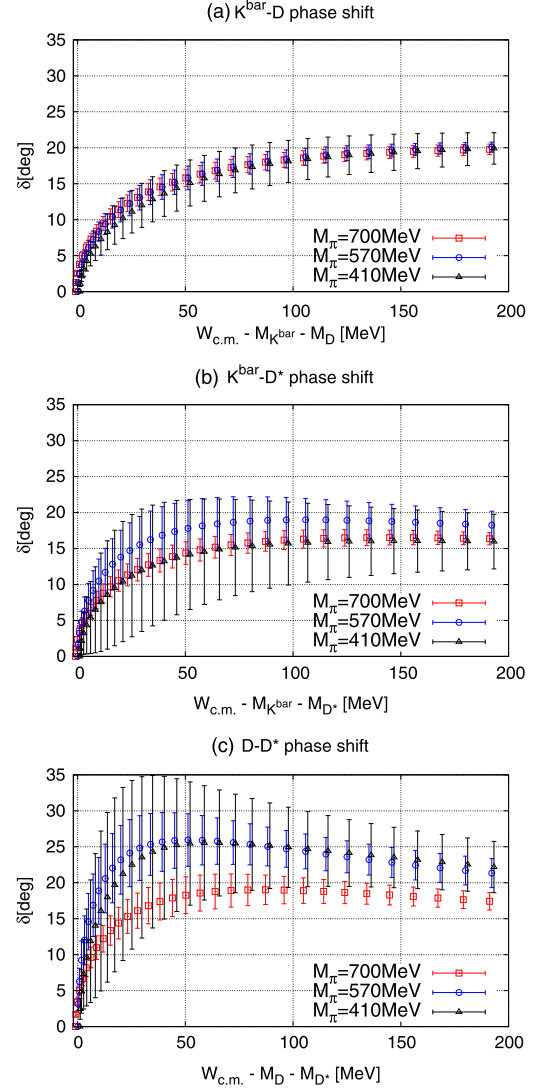


Fig. 3. (Color online.) S-wave $I = 0$ scattering phase shifts in the (a) $\bar{K}\text{--}D$, (b) $\bar{K}\text{--}D^*$ and (c) $D\text{--}D^*$ channels. Vertical error bars represent both statistical and systematic errors.

Although we find a good evidence of a sizable attraction in the $I = 0$ channel at $m_\pi = 410\text{--}700$ MeV, the existence of a bound or resonant $T_{cc}(J^P = 1^+, I = 0)$ at the physical point remains an open question.³

5. Summary

In order to clarify the possible existence of charmed tetraquark states (T_{cc} and T_{cs}), we have studied the S-wave meson–meson interactions in several $I = 0$ and $I = 1$ channels ($D\text{--}D$, $\bar{K}\text{--}D$, $D\text{--}D^*$ and $\bar{K}\text{--}D^*$), using $(2+1)$ -flavor full QCD gauge configurations generated at $m_\pi = 410\text{--}700$ MeV. For the charm quark, we have employed the relativistic heavy-quark action to take into account its dynamics on the lattice.

S-wave meson–meson potentials are extracted from Nambu–Bethe–Salpeter wave functions using the HAL QCD method. Potentials are then used to calculate scattering phase shifts and

³ If we take the same attractive potential as $D\text{--}D^*$ ($J^P = 1^+, I = 0$) at $m_\pi = 410$ MeV and calculate the $B\text{--}B^*$ ($J^P = 1^+, I = 0$) channel with the physical masses of B and B^* , we find a bound state with the binding energy 5.7(2.3) MeV.

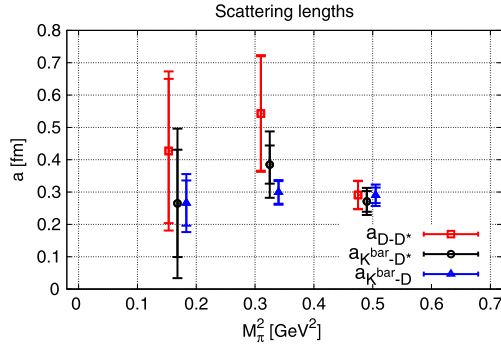


Fig. 4. (Color online.) Pion mass dependences of scattering lengths in the $I = 0$ $\bar{K}-D$, $\bar{K}-D^*$ and $D-D^*$ channels. Inner vertical error bars represent statistical errors. Both statistical and systematic errors are included in total error bars.

Table 4

Scattering lengths in the $I = 0$ channels for the $\bar{K}-D$, $\bar{K}-D^*$ and $D-D^*$ systems. The statistical and systematic errors are also shown.

m_π (MeV)	411(2)	572(2)	699(1)
$a_{\bar{K}D}$ (fm)	0.266(70)(56)	0.299(35)(15)	0.290(24)(23)
$a_{\bar{K}D^*}$ (fm)	0.265(166)(161)	0.385(59)(84)	0.271(32)(27)
a_{DD^*} (fm)	0.427(223)(104)	0.543(177)(35)	0.291(43)(10)

scattering lengths. S-wave meson–meson interactions in the $I = 1$ channels are found to be repulsive and insensitive to the pion mass in the region we explored, so that tetraquark bound states are unlikely to be formed even at the physical pion mass. On the other hand, the S-wave interactions in the $I = 0$ channels show attractions in the $\bar{K}-D$, $\bar{K}-D^*$ and $D-D^*$ channels, which are qualitatively consistent with the phenomenological diquark picture. S-wave scattering phase shifts in these attractive channels indicate, however, that no bound states or resonances are formed at the pion masses used in this study, $m_\pi = 410\text{--}700$ MeV, though attractions become more prominent as the pion mass decreases, particularly in the $I = 0$ $D-D^*$ channel corresponding to T_{cc} ($J^P = 1^+, I = 0$).

To make a definite conclusion on the fate of T_{cc} and T_{cs} in the real world, simulations near or at the physical point are necessary. We are planning to carry out such simulations with the PACS-CS (2 + 1)-flavor full QCD configurations with coupled-channel schemes [26,30].

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